

**Write an equation for the quadratic function whose graph contains the given characteristics.**

1. has a  $y$ -intercept of 4 and the point  $(2, 0)$  is the vertex
2. has  $x$ -intercepts at  $(-4, 0)$  and  $(0, 0)$  and the point  $(-2, 4)$  is the vertex
3. passes through the point  $(1, 2)$  and the point  $(3, 4)$  is the vertex
4. passes through the points  $(1, 0)$ ,  $(4, 3)$ , and  $(5, 8)$
5. passes through the points  $(-2, 7)$ ,  $(0, 1)$ , and  $(8, 17)$
6. Among all the rectangles whose perimeters are 100 feet, find the dimensions of the one with maximum area.
7. A farmer wants to put a fence around a rectangular garden. Only 3 sides must be fenced, since a rock wall will form the fourth side. If he uses 60m of fencing, what is the maximum area possible?
8. Find two positive real numbers whose product is a maximum. The sum of the first and three times the second is 30.
9. A manufacturer of lighting fixtures has daily production costs of  $C = 800 - 10x + 0.20x^2$ , where  $C$  is the total cost (in dollars) and  $x$  is the number of units produced. How many fixtures should be produced each day to yield a minimum cost?

**Find all the zeros of the function.**

10.  $f(x) = x^3 - 2x^2 + 20x - 40$
11.  $f(x) = 6x^3 + x^2 - 4x + 1$
12.  $f(x) = x^3 - x^2 - 8x + 8$
13.  $f(x) = x^4 + x^3 - 16x^2 + 4x - 80$
14.  $f(x) = x^4 + x^3 - 13x^2 - 7x + 30$

**Write a least degree polynomial given the zeros (roots) of the function.**

15.  $x = -2, -\frac{1}{3}, -\frac{1}{5}$
16.  $x = 4, \pm\sqrt{3}$
17.  $x = 4, -5, 2i$
18. Use function composition to prove algebraically that  $f(x)$  and  $g(x)$  are inverses of one another.  
 $f(x) = 7x + 4$   
 $g(x) = \frac{1}{7}x - \frac{4}{7}$